



Nonlinear Photonics with Optical Waveguides

Govind P. Agrawal

The Institute of Optics
University of Rochester
Rochester, New York, USA



Outline

- Introduction
- Planar and Cylindrical Waveguides
- Chromatic dispersion and Kerr Nonlinearity
- Self-Phase Modulation
- Cross-Phase Modulation
- Four-Wave Mixing
- Stimulated Raman Scattering
- Stimulated Brillouin Scattering



2/44

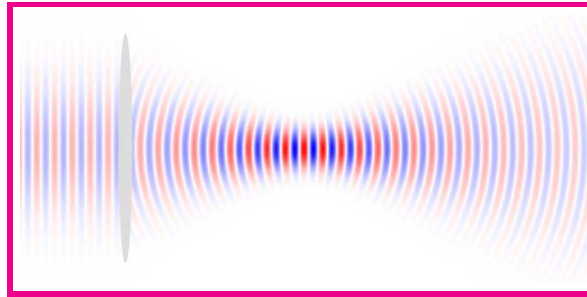


Back

Close

Introduction

- Nonlinear optical effects have been studied since 1962 and have found applications in many branches of optics.



- Nonlinear interaction length is limited in bulk materials because of tight focusing and diffraction of optical beams:

$$L_{\text{diff}} = kw_0^2, \quad (k = 2\pi/\lambda).$$

- Much longer interaction lengths become feasible in optical waveguides, which confine light through total internal reflection.
- Optical fibers allow interaction lengths > 1 km.





Advantage of Waveguides

- Efficiency of a nonlinear process in bulk media is governed by

$$(I_0 L_{\text{int}})_{\text{bulk}} = \left(\frac{P_0}{\pi w_0^2} \right) \frac{\pi w_0^2}{\lambda} = \frac{P_0}{\lambda}.$$

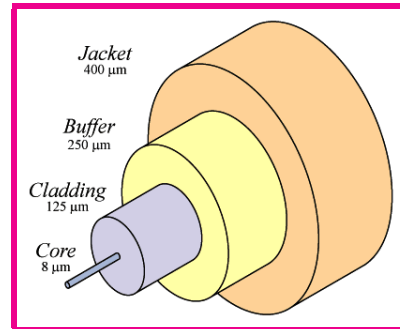
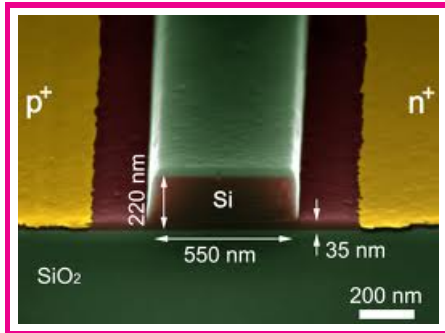
- In a waveguide, spot size w_0 remains constant across its length L .
- In this situation L_{int} is limited by the waveguide loss α .
- Using $I(z) = I_0 e^{-\alpha z}$, we obtain

$$(I_0 L_{\text{int}})_{\text{wg}} = \int_0^L I_0 e^{-\alpha z} dz \approx \frac{P_0}{\pi w_0^2 \alpha}.$$

- Nonlinear efficiency in a waveguide can be improved by

$$\frac{(I_0 L_{\text{int}})_{\text{wg}}}{(I_0 L_{\text{int}})_{\text{bulk}}} = \frac{\lambda}{\pi w_0^2 \alpha} \sim 10^6.$$

Planar and Cylindrical Waveguides



- Dielectric waveguides employ total internal reflection to confine light to a central region.
- The refractive index is larger inside this central region.
- Two main classes: Planar and cylindrical waveguides.
- In the planar case, a ridge structure used for 2-D confinement.
- Optical fibers dope silica glass with germanium to realize a central core with slightly higher refractive index.



Light Propagation in Waveguides

- Optical pulses launched into optical waveguides are affected by (i) optical losses, (ii) dispersion, and (iii) Kerr nonlinearity.
- Losses are negligible in optical fibers (< 0.5 dB/km) and manageable (< 1 dB/cm) in planar waveguides.
- Dispersion can be normal or anomalous but its value can be tailored through waveguide design.
- The combination of dispersion and nonlinearity leads to a variety of nonlinear phenomena with useful applications.
- Optical fibers used often in practice because their low losses allow long interaction lengths.
- Planar waveguides made using silicon, silicon nitride, or chalcogenide glasses are attracting attention in recent years.



6/44



Back

Close

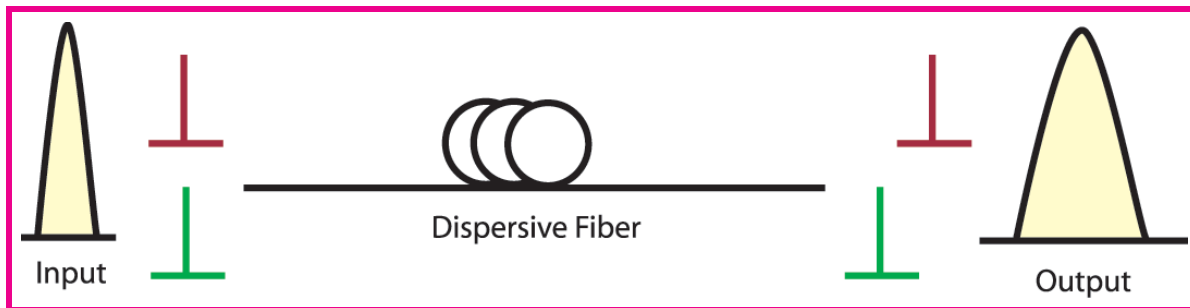
Chromatic Dispersion

- Frequency dependence of the propagation constant included using

$$\beta(\omega) = \bar{n}(\omega)\omega/c = \beta_0 + \beta_1(\omega - \omega_0) + \beta_2(\omega - \omega_0)^2 + \dots,$$

where ω_0 is the carrier frequency of optical pulse.

- Group velocity is related to $\beta_1 = (d\beta/d\omega)_{\omega=\omega_0}$ as $v_g = 1/\beta_1$.
- Different frequency components of a pulse travel at different speeds and result in pulse broadening governed by $\beta_2 = (d^2\beta/d\omega^2)_{\omega=\omega_0}$.



7/44

Waveguide Dispersion

- Mode index $\bar{n}(\omega) = n_1(\omega) - \delta n_W(\omega)$.
- Material dispersion included through $n_1(\omega)$ of the core.
- Waveguide dispersion results from $\delta n_W(\omega)$ and depends on the waveguide design and dimensions.
- Total dispersion $\beta_2 = \beta_{2M} + \beta_{2W}$ can be controlled by changing design of a waveguide.
- β_2 vanishes at a specific wavelength known as the *zero-dispersion wavelength* (ZDWL).
- This wavelength separates the *normal* ($\beta_2 > 0$) and *anomalous* ($\beta_2 < 0$) dispersion regions of a waveguide.
- Some fibers exhibit multiple zero-dispersion wavelengths.



8/44



Back

Close

Major Nonlinear Effects

- Self-Phase Modulation (SPM)
- Cross-Phase Modulation (XPM)
- Four-Wave Mixing (FWM)
- Stimulated Brillouin Scattering (SBS)
- Stimulated Raman Scattering (SRS)

Origin of Nonlinear Effects

- Third-order nonlinear susceptibility $\chi^{(3)}$.
- Real part leads to SPM, XPM, and FWM.
- Imaginary part leads to two-photon absorption (TPA).



9/44



Back

Close



Third-order Nonlinear Susceptibility

- The tensorial nature of $\chi^{(3)}$ makes theory quite complicated.
- It can be simplified considerably when a single optical beam excites the fundamental mode of an optical waveguide.
- Only the component $\chi_{1111}^{(3)}(-\omega; \omega, -\omega, \omega)$ is relevant in this case.
- Its real and imaginary parts provide the Kerr coefficient n_2 and the TPA coefficient β_T as

$$n_2(\omega) + \frac{ic}{2\omega}\beta_{\text{TPA}}(\omega) = \frac{3}{4\epsilon_0 cn_0^2}\chi_{1111}^{(3)}(-\omega; \omega, -\omega, \omega).$$

- A 2007 review on silicon waveguides provides more details:
Q. Lin, O. Painter, G. P. Agrawal, Opt. Express **15**, 16604 (2007).



Back

Close

Nonlinear Parameters

- Refractive index depends on intensity as (Kerr effect):

$$n(\omega, I) = \bar{n}(\omega) + n_2(1 + ir)I(t).$$

- Material parameter $n_2 = 3 \times 10^{-18} \text{ m}^2/\text{W}$ is larger for silicon by a factor of 100 compared with silica fibers.
- Dimensionless parameter $r = \beta_{\text{TPA}}/(2k_0n_2)$ is related to two-photon absorption (TPA).
- For silicon $\beta_{\text{TPA}} = 5 \times 10^{-12} \text{ m}/\text{W}$ at wavelengths near 1550 nm.
- Dimensionless parameter $r \approx 0.1$ for silicon near 1550 nm.
- Negligible TPA occurs in silica glasses ($r \approx 0$).
- TPA is not negligible for chalcogenide glasses ($r \approx 0.2$).



11/44



Back

Close

Self-Phase Modulation

- In silica fibers, refractive index depends on intensity as

$$n(\omega, I) = \bar{n}(\omega) + n_2 I(t).$$

- Frequency dependence of \bar{n} leads to dispersion.
- Using $\phi = (2\pi/\lambda)nL$, I dependence of n leads to nonlinear phase shift

$$\phi_{\text{NL}}(t) = (2\pi/\lambda)n_2 I(t)L = \gamma P(t)L.$$

- Clearly, the optical field modifies its own phase (hence, SPM).
- For pulses, phase shift varies with time (leads to chirping).
- As the pulse propagates down the fiber, its spectrum changes because of SPM induced by the Kerr effect.



12/44



Back

Close

Nonlinear Phase Shift

- Pulse propagation governed by the Nonlinear Schrödinger Equation

$$i \frac{\partial A}{\partial z} - \frac{\beta_2}{2} \frac{\partial^2 A}{\partial t^2} + \gamma |A|^2 A = 0.$$

- Dispersive effects within the fiber included through β_2 .
- Nonlinear effects included through $\gamma = 2\pi n_2 / (\lambda A_{\text{eff}})$.
- If we ignore dispersive effects, solution can be written as

$$A(L, t) = A(0, t) \exp(i\phi_{\text{NL}}), \quad \text{where} \quad \phi_{\text{NL}}(t) = \gamma L |A(0, t)|^2.$$

- Nonlinear phase shift depends on input pulse shape.
- Maximum Phase shift: $\phi_{\text{max}} = \gamma P_0 L = L / L_{\text{NL}}$.
- Nonlinear length: $L_{\text{NL}} = (\gamma P_0)^{-1} \sim 1 \text{ km}$ for $P_0 \sim 1 \text{ W}$.



13/44



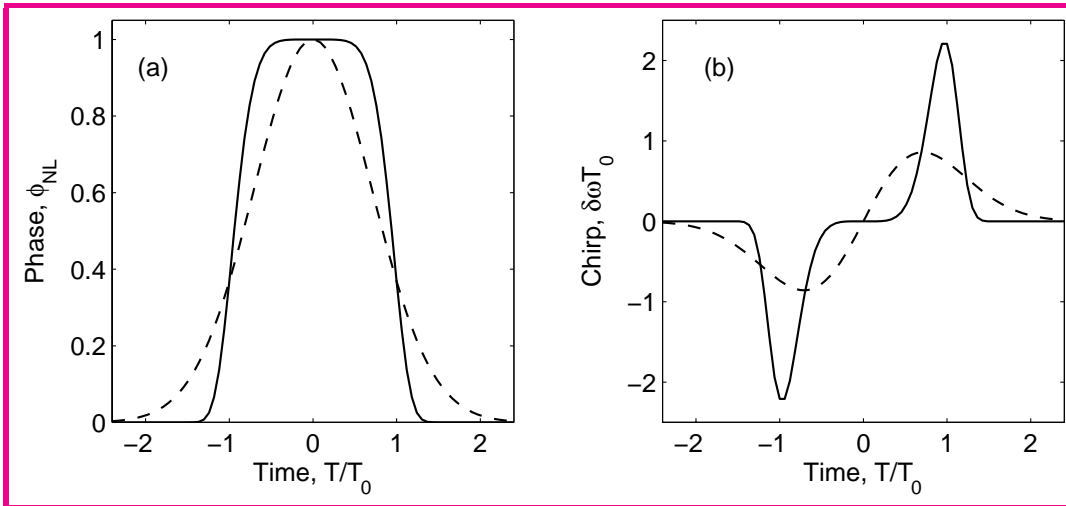
Back

Close

SPM-Induced Chirp



14/44



- Super-Gaussian pulses: $P(t) = P_0 \exp[-(t/T)^{2m}]$.
- Gaussian pulses correspond to the choice $m = 1$.
- Chirp is related to the phase derivative $d\phi/dt$.
- SPM creates new frequencies and leads to spectral broadening.

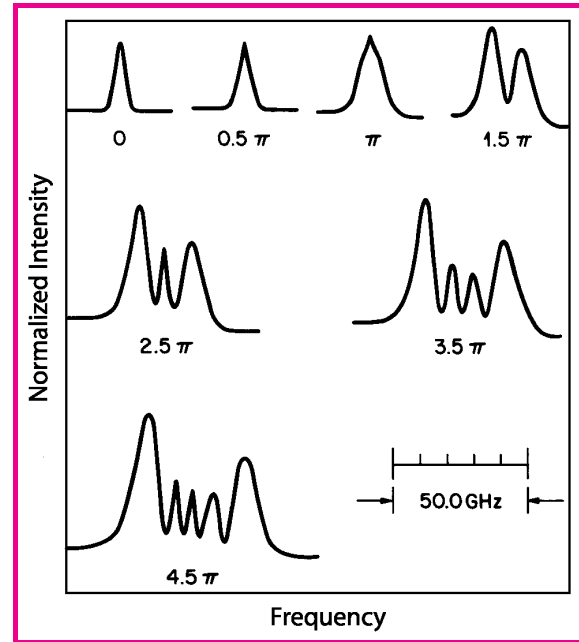


SPM-Induced Spectral Broadening



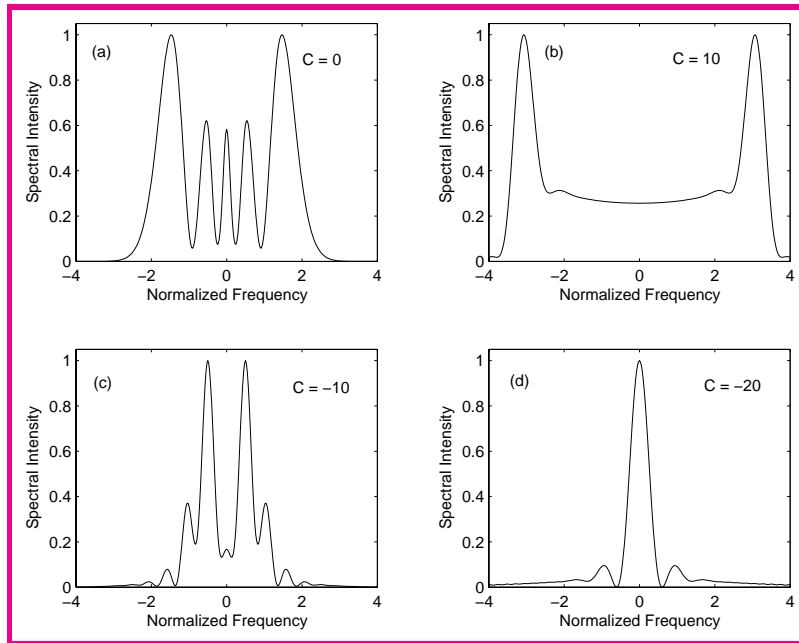
15/44

- First observed in 1978 by Stolen and Lin.
- 90-ps pulses transmitted through a 100-m-long fiber.
- Spectra are labelled using $\phi_{\max} = \gamma P_0 L$.
- Number M of spectral peaks: $\phi_{\max} = (M - \frac{1}{2})\pi$.



- Output spectrum depends on shape and chirp of input pulses.
- Even spectral compression can occur for suitably chirped pulses.

SPM-Induced Spectral Narrowing



- Chirped Gaussian pulses with $A(0, t) = A_0 \exp[-\frac{1}{2}(1 + iC)(t/T_0)^2]$.
- If $C < 0$ initially, SPM produces spectral narrowing.



16/44



SPM: Good or Bad?

- SPM-induced spectral broadening can degrade performance of a lightwave system.
- Modulation instability often enhances system noise.

On the positive side . . .

- Modulation instability can be used to produce ultrashort pulses at high repetition rates.
- SPM often used for fast optical switching (NOLM or MZI).
- Formation of standard and dispersion-managed optical solitons.
- Useful for all-optical regeneration of WDM channels.
- Other applications (pulse compression, chirped-pulse amplification, passive mode-locking, etc.)



17/44



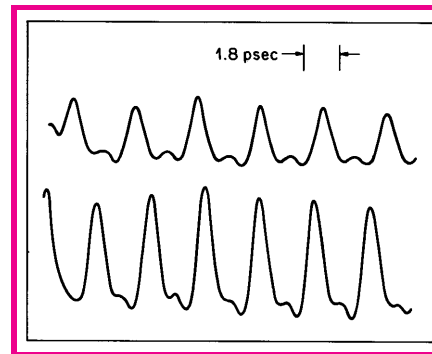
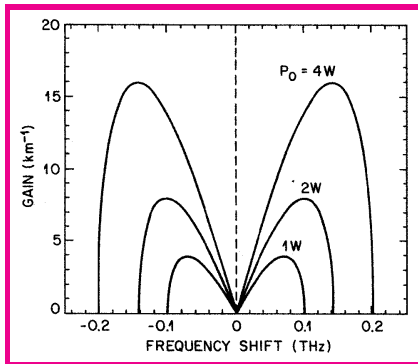
Back

Close

Modulation Instability

Nonlinear Schrödinger Equation

$$i \frac{\partial A}{\partial z} - \frac{\beta_2}{2} \frac{\partial^2 A}{\partial t^2} + \gamma |A|^2 A = 0.$$

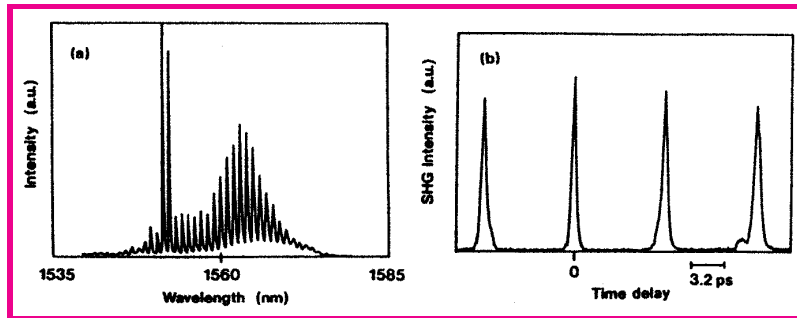


- CW solution unstable for anomalous dispersion ($\beta_2 < 0$).
- Useful for producing ultrashort pulse trains at tunable repetition rates [Tai et al., PRL 56, 135 (1986); APL 49, 236 (1986)].



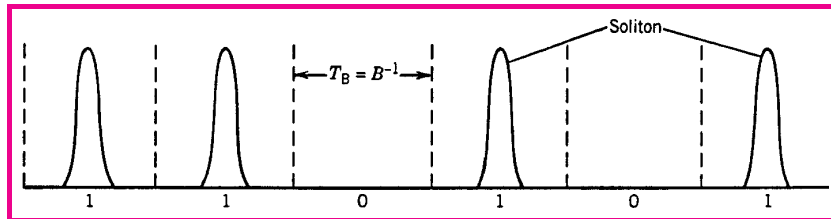
Modulation Instability (cont.)

- A CW beam can be converted into a pulse train.
- Two CW beams at slightly different wavelengths can initiate modulation instability and allow tuning of pulse repetition rate.
- Repetition rate is governed by their wavelength difference.
- Repetition rates ~ 100 GHz realized by 1993 using DFB lasers (Chernikov et al., APL 63, 293, 1993).



Optical Solitons

- Combination of SPM and anomalous GVD produces solitons.
- Solitons preserve their shape in spite of the dispersive and nonlinear effects occurring inside fibers.
- Useful for optical communications systems.



- Dispersive and nonlinear effects balanced when $L_{NL} = L_D$.
- Nonlinear length $L_{NL} = 1/(\gamma P_0)$; Dispersion length $L_D = T_0^2/|\beta_2|$.
- Two lengths become equal if peak power and width of a pulse satisfy $P_0 T_0^2 = |\beta_2|/\gamma$.

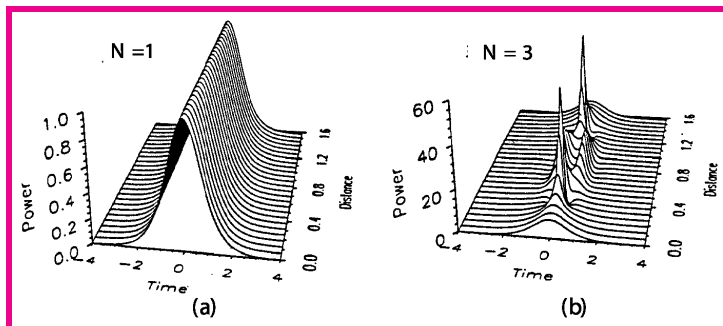


Fundamental and Higher-Order Solitons

- NLS equation: $i\frac{\partial A}{\partial z} - \frac{\beta_2}{2}\frac{\partial^2 A}{\partial t^2} + \gamma|A|^2A = 0$.
- Solution depends on a single parameter: $N^2 = \frac{\gamma P_0 T_0^2}{|\beta_2|}$.
- Fundamental ($N = 1$) solitons preserve shape:

$$A(z, t) = \sqrt{P_0} \operatorname{sech}(t/T_0) \exp(iz/2L_D).$$

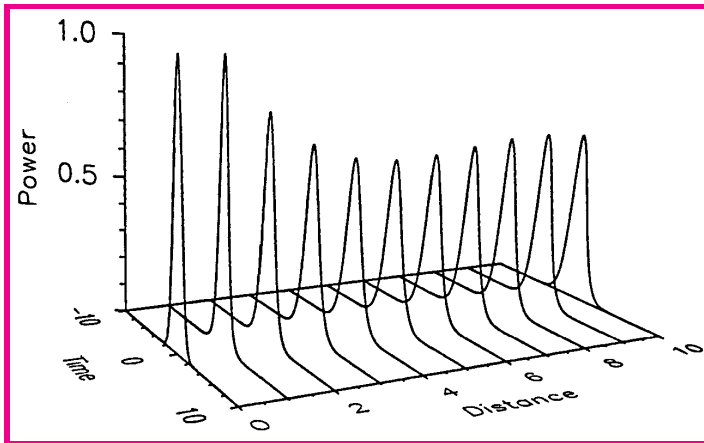
- Higher-order solitons evolve in a periodic fashion.





Stability of Optical Solitons

- Solitons are remarkably stable.
- Fundamental solitons can be excited with any pulse shape.



Gaussian pulse with $N = 1$.
Pulse eventually acquires
a 'sech' shape.

- Can be interpreted as temporal modes of a SPM-induced waveguide.
- $\Delta n = n_2 I(t)$ larger near the pulse center.
- Some pulse energy is lost through dispersive waves.



23/44

Cross-Phase Modulation

- Consider two optical fields propagating simultaneously.
- Nonlinear refractive index seen by one wave depends on the intensity of the other wave as

$$\Delta n_{\text{NL}} = n_2(|A_1|^2 + b|A_2|^2).$$

- Total nonlinear phase shift:

$$\phi_{\text{NL}} = (2\pi L/\lambda)n_2[I_1(t) + bI_2(t)].$$

- An optical beam modifies not only its own phase but also of other copropagating beams (XPM).
- XPM induces nonlinear coupling among overlapping optical pulses.



Back

Close

XPM: Good or Bad?

- XPM leads to interchannel crosstalk in WDM systems.
- It can produce amplitude and timing jitter.

On the other hand ...

XPM can be used beneficially for

- Nonlinear Pulse Compression
- Passive mode locking
- Ultrafast optical switching
- Demultiplexing of OTDM channels
- Wavelength conversion of WDM channels



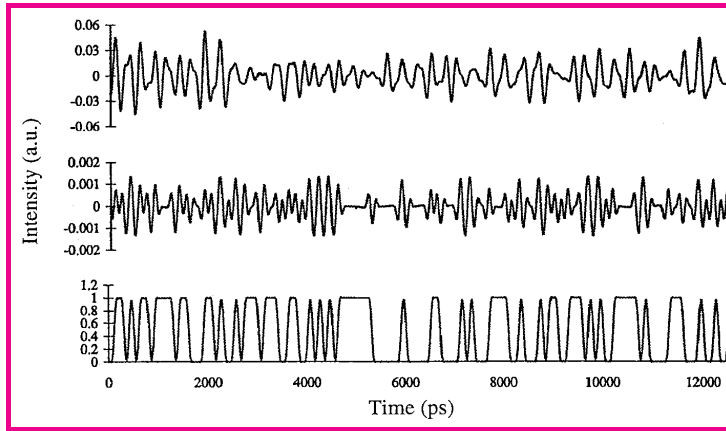
24/44



Back

Close

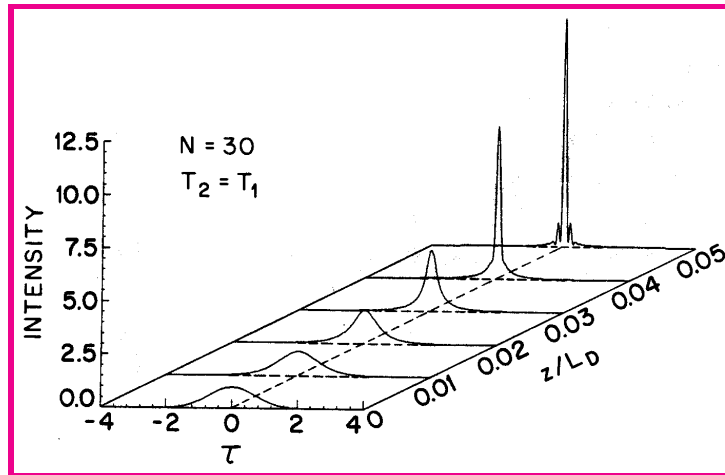
XPM-Induced Crosstalk



- A CW probe propagated with 10-Gb/s pump channel.
- Probe phase modulated through XPM.
- Dispersion converts phase modulation into amplitude modulation.
- Probe power after 130 (middle) and 320 km (top) exhibits large fluctuations (Hui et al., JLT, 1999).



XPM-Induced Pulse Compression



- An intense pump pulse is copropagated with the low-energy pulse requiring compression.
- Pump produces XPM-induced chirp on the weak pulse.
- Fiber dispersion compresses the pulse.



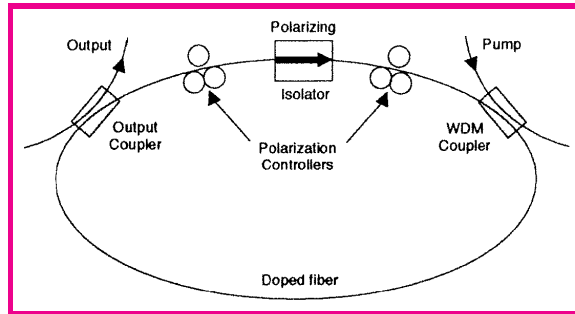
26/44



Back

Close

XPM-Induced Mode Locking



- Different nonlinear phase shifts for the two polarization components: **nonlinear polarization rotation**.

$$\phi_x - \phi_y = (2\pi L/\lambda)n_2[(I_x + bI_y) - (I_y + bI_x)].$$

- Pulse center and wings develop different polarizations.
- Polarizing isolator clips the wings and shortens the pulse.
- Can produce ~ 100 fs pulses.



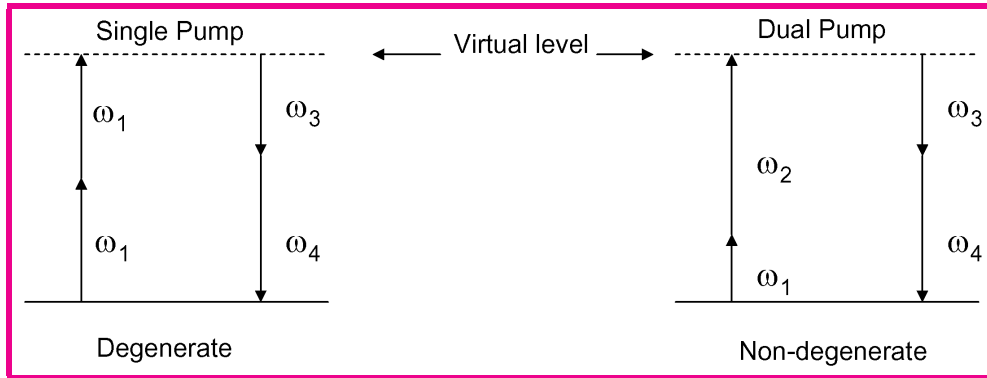
27/44



Back

Close

Four-Wave Mixing (FWM)



- FWM is a nonlinear process that transfers energy from pumps to signal and idler waves.
- FWM requires conservation of (notation: $E = \text{Re}[Ae^{i(\beta z - \omega t)}]$)
 - ★ Energy $\omega_1 + \omega_2 = \omega_3 + \omega_4$
 - ★ Momentum $\beta_1 + \beta_2 = \beta_3 + \beta_4$
- Degenerate FWM: Single pump ($\omega_1 = \omega_2$).





Theory of Four-Wave Mixing

- Third-order polarization: $\mathbf{P}_{\text{NL}} = \epsilon_0 \chi^{(3)} : \mathbf{E} \mathbf{E} \mathbf{E}$ (Kerr nonlinearity).

$$\mathbf{E} = \frac{1}{2} \hat{x} \sum_{j=1}^4 F_j(x, y) A_j(z, t) \exp[i(\beta_j z - \omega_j t)] + \text{c.c.}$$

- The four slowly varying amplitudes satisfy

$$\frac{dA_1}{dz} = \frac{in_2\omega_1}{c} \left[\left(f_{11}|A_1|^2 + 2 \sum_{k \neq 1} f_{1k}|A_k|^2 \right) A_1 + 2f_{1234}A_2^*A_3A_4 e^{i\Delta kz} \right]$$

$$\frac{dA_2}{dz} = \frac{in_2\omega_2}{c} \left[\left(f_{22}|A_2|^2 + 2 \sum_{k \neq 2} f_{2k}|A_k|^2 \right) A_2 + 2f_{2134}A_1^*A_3A_4 e^{i\Delta kz} \right]$$

$$\frac{dA_3}{dz} = \frac{in_2\omega_3}{c} \left[\left(f_{33}|A_3|^2 + 2 \sum_{k \neq 3} f_{3k}|A_k|^2 \right) A_3 + 2f_{3412}A_1A_2A_4^* e^{-i\Delta kz} \right]$$

$$\frac{dA_4}{dz} = \frac{in_2\omega_4}{c} \left[\left(f_{44}|A_4|^2 + 2 \sum_{k \neq 4} f_{4k}|A_k|^2 \right) A_4 + 2f_{4312}A_1A_2A_3^* e^{-i\Delta kz} \right]$$



Simplified FWM Theory

- Full problem quite complicated (4 coupled nonlinear equations)
- Overlap integrals $f_{ijkl} \approx f_{ij} \approx 1/A_{\text{eff}}$ in single-mode fibers.
- Linear phase mismatch: $\Delta k = \beta(\omega_3) + \beta(\omega_4) - \beta(\omega_1) - \beta(\omega_2)$.
- Undepleted-pump approximation simplifies the problem.
- Using $A_j = B_j \exp[2i\gamma(P_1 + P_2)z]$, the signal and idler satisfy

$$\frac{dB_3}{dz} = 2i\gamma\sqrt{P_1 P_2} B_4^* e^{-ikz}, \quad \frac{dB_4}{dz} = 2i\gamma\sqrt{P_1 P_2} B_3^* e^{-ikz}.$$

- Signal power P_3 and Idler power P_4 are much smaller than pump powers P_1 and P_2 ($P_n = |A_n|^2 = |B_n|^2$).
- Total phase mismatch: $\kappa = \beta_3 + \beta_4 - \beta_1 - \beta_2 + \gamma(P_1 + P_2)$.
- Nonlinear parameter: $\gamma = n_2\omega_0/(cA_{\text{eff}}) \sim 10 \text{ W}^{-1}/\text{km}$.



30/44



Back

Close



General Solution

- Signal and idler fields satisfy coupled linear equations

$$\frac{dB_3}{dz} = 2i\gamma\sqrt{P_1P_2}B_4^*e^{-i\kappa z}, \quad \frac{dB_4^*}{dz} = -2i\gamma\sqrt{P_1P_2}B_3e^{i\kappa z}.$$

- General solution when both the signal and idler are present at $z = 0$:

$$B_3(z) = \{B_3(0)[\cosh(gz) + (i\kappa/2g)\sinh(gz)] + (i\gamma/g)\sqrt{P_1P_2}B_4^*(0)\sinh(gz)\}e^{-i\kappa z/2}$$

$$B_4^*(z) = \{B_4^*(0)[\cosh(gz) - (i\kappa/2g)\sinh(gz)] - (i\gamma/g)\sqrt{P_1P_2}B_3(0)\sinh(gz)\}e^{i\kappa z/2}$$

- If an idler is not launched at $z = 0$ (phase-insensitive amplification):

$$B_3(z) = B_3(0)[\cosh(gz) + (i\kappa/2g)\sinh(gz)]e^{-i\kappa z/2}$$

$$B_4^*(z) = B_3(0)(-i\gamma/g)\sqrt{P_1P_2}\sinh(gz)e^{i\kappa z/2}$$



Gain Spectrum

- Signal amplification factor for a FOPA:

$$G(\omega) = \frac{P_3(L, \omega)}{P_3(0, \omega)} = \left[1 + \left(1 + \frac{\kappa^2(\omega)}{4g^2(\omega)} \right) \sinh^2[g(\omega)L] \right].$$

- Parametric gain: $g(\omega) = \sqrt{4\gamma^2 P_1 P_2 - \kappa^2(\omega)}/4$.
- Wavelength conversion efficiency:

$$\eta_c(\omega) = \frac{P_4(L, \omega)}{P_3(0, \omega)} = \left(1 + \frac{\kappa^2(\omega)}{4g^2(\omega)} \right) \sinh^2[g(\omega)L].$$

- Best performance for perfect phase matching ($\kappa = 0$):

$$G(\omega) = \cosh^2[g(\omega)L], \quad \eta_c(\omega) = \sinh^2[g(\omega)L].$$



32/44



Back

Close

FWM: Good or Bad?

- FWM leads to interchannel crosstalk in WDM systems.
- It generates additional noise and degrades system performance.

On the other hand ...

FWM can be used beneficially for

- Optical amplification and wavelength conversion
- Phase conjugation and dispersion compensation
- Ultrafast optical switching and signal processing
- Generation of correlated photon pairs



33/44



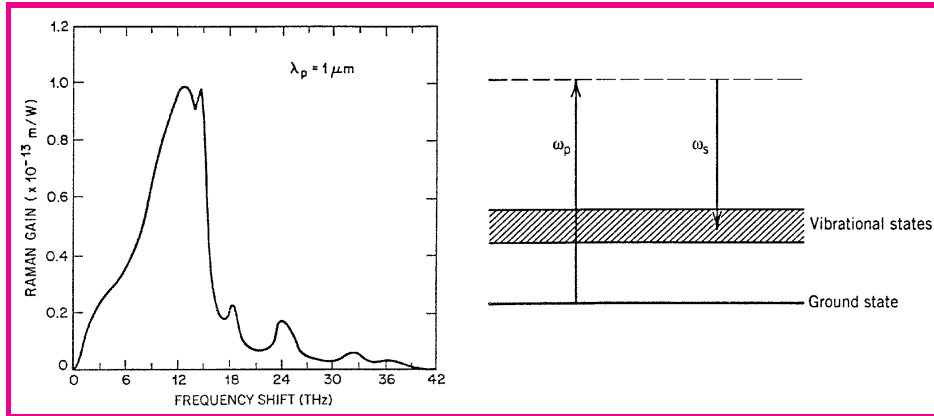
Back

Close



Stimulated Raman Scattering

- Scattering of light from vibrating silica molecules.
- Amorphous nature of silica turns vibrational state into a band.
- Raman gain spectrum extends over 40 THz or so.



- Raman gain is maximum near 13 THz.
- Scattered light red-shifted by 100 nm in the 1.5 μm region.

Raman Threshold

- Raman threshold is defined as the input pump power at which Stoke power becomes equal to the pump power at the fiber output:

$$P_s(L) = P_p(L) \equiv P_0 \exp(-\alpha_p L).$$

- Using $P_{s0}^{\text{eff}} = (\hbar\omega_s)B_{\text{eff}}$, the Raman threshold condition becomes

$$P_{s0}^{\text{eff}} \exp(g_R P_0 L_{\text{eff}} / A_{\text{eff}}) = P_0,$$

- Assuming a Lorentzian shape for the Raman-gain spectrum, Raman threshold is reached when (Smith, Appl. Opt. **11**, 2489, 1972)

$$\frac{g_R P_{th} L_{\text{eff}}}{A_{\text{eff}}} \approx 16 \quad \Longrightarrow \quad P_{th} \approx \frac{16 A_{\text{eff}}}{g_R L_{\text{eff}}}.$$



35/44



Back

Close



36/44

Estimates of Raman Threshold

Telecommunication Fibers

- For long fibers, $L_{\text{eff}} = [1 - \exp(-\alpha L)]/\alpha \approx 1/\alpha \approx 20$ km for $\alpha = 0.2$ dB/km at $1.55 \mu\text{m}$.
- For telecom fibers, $A_{\text{eff}} = 50\text{--}75 \mu\text{m}^2$.
- Threshold power $P_{th} \sim 1$ W is too large to be of concern.
- Interchannel crosstalk in WDM systems because of Raman gain.

Yb-doped Fiber Lasers and Amplifiers

- Because of gain, $L_{\text{eff}} = [\exp(gL) - 1]/g > L$.
- For fibers with a large core, $A_{\text{eff}} \sim 1000 \mu\text{m}^2$.
- P_{th} exceeds 10 kW for short fibers ($L < 10$ m).
- SRS may limit fiber lasers and amplifiers if $L \gg 10$ m.



Back

Close

SRS: Good or Bad?

- Raman gain introduces interchannel crosstalk in WDM systems.
- Crosstalk can be reduced by lowering channel powers but it limits the number of channels.

On the other hand ...

- Raman amplifiers are a boon for WDM systems.
- Can be used in the entire 1300–1650 nm range.
- EDFA bandwidth limited to ~ 40 nm near 1550 nm.
- Distributed nature of Raman amplification lowers noise.
- Needed for opening new transmission bands in telecom systems.



37/44



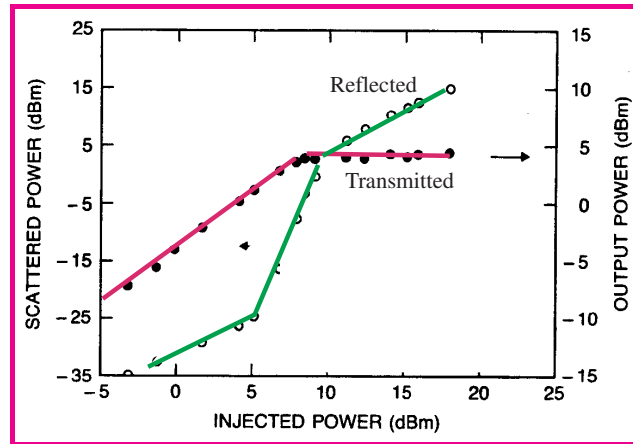
Back

Close



Stimulated Brillouin Scattering

- Originates from scattering of light from acoustic waves.
- Becomes a stimulated process when input power exceeds a threshold level.
- Threshold power relatively low for long fibers (~ 5 mW).



- Most of the power reflected backward after SBS threshold is reached.

Brillouin Shift

- Pump produces density variations through electrostriction.
- Resulting index grating generates Stokes wave through Bragg diffraction.
- Energy and momentum conservations require:

$$\Omega_B = \omega_p - \omega_s, \quad \vec{k}_A = \vec{k}_p - \vec{k}_s.$$

- Acoustic waves satisfy the dispersion relation:

$$\Omega_B = v_A |\vec{k}_A| \approx 2v_A |\vec{k}_p| \sin(\theta/2).$$

- In a single-mode fiber $\theta = 180^\circ$, resulting in

$$v_B = \Omega_B / 2\pi = 2n_p v_A / \lambda_p \approx 11 \text{ GHz},$$

if we use $v_A = 5.96 \text{ km/s}$, $n_p = 1.45$, and $\lambda_p = 1.55 \text{ } \mu\text{m}$.



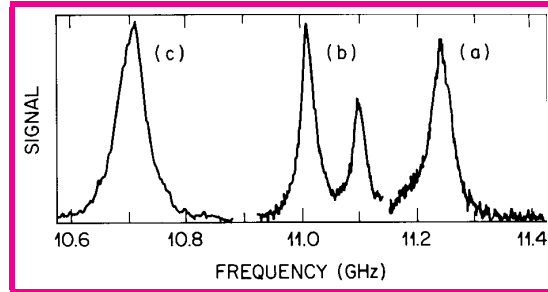
39/44



Back

Close

Brillouin Gain Spectrum



- Measured spectra for (a) silica-core (b) depressed-cladding, and (c) dispersion-shifted fibers.
- Brillouin gain spectrum is quite narrow (~ 50 MHz).
- Brillouin shift depends on GeO_2 doping within the core.
- Multiple peaks are due to the excitation of different acoustic modes.
- Each acoustic mode propagates at a different velocity v_A and thus leads to a different Brillouin shift ($v_B = 2n_p v_A / \lambda_p$).



40/44



Back

Close

Brillouin Threshold

- Pump and Stokes evolve along the fiber as

$$-\frac{dI_s}{dz} = g_B I_p I_s - \alpha I_s, \quad \frac{dI_p}{dz} = -g_B I_p I_s - \alpha I_p.$$

- Ignoring pump depletion, $I_p(z) = I_0 \exp(-\alpha z)$.
- Solution of the Stokes equation:

$$I_s(L) = I_s(0) \exp(g_B I_0 L_{\text{eff}} - \alpha L).$$

- Brillouin threshold is obtained from

$$\frac{g_B P_{th} L_{\text{eff}}}{A_{\text{eff}}} \approx 21 \quad \implies \quad P_{th} \approx \frac{21 A_{\text{eff}}}{g_B L_{\text{eff}}}.$$

- Brillouin gain $g_B \approx 5 \times 10^{-11}$ m/W is nearly independent of the pump wavelength.



41/44



Back

Close

Estimates of Brillouin Threshold

Telecommunication Fibers

- For long fibers, $L_{\text{eff}} = [1 - \exp(-\alpha L)]/\alpha \approx 1/\alpha \approx 20$ km for $\alpha = 0.2$ dB/km at $1.55 \mu\text{m}$.
- For telecom fibers, $A_{\text{eff}} = 50\text{--}75 \mu\text{m}^2$.
- Threshold power $P_{th} \sim 1$ mW is relatively small.

Yb-doped Fiber Lasers and Amplifiers

- P_{th} exceeds 20 W for a 1-m-long standard fibers.
- Further increase occurs for large-core fibers; $P_{th} \sim 400$ W when $A_{\text{eff}} \sim 1000 \mu\text{m}^2$.
- SBS is the dominant limiting factor at power levels $P_0 > 0.5$ kW.



42/44



Back

Close



43/44

Techniques for Controlling SBS

- Pump-Phase modulation: Sinusoidal modulation at several frequencies >0.1 GHz or with a pseudorandom bit pattern.
- Cross-phase modulation by launching a pseudorandom pulse train at a different wavelength.
- Temperature gradient along the fiber: Changes in $v_B = 2n_p v_A / \lambda_p$ through temperature dependence of n_p .
- Built-in strain along the fiber: Changes in v_B through n_p .
- Nonuniform core radius and dopant density: mode index n_p also depends on fiber design parameters (a and Δ).
- Control of overlap between the optical and acoustic modes.
- Use of Large-core fibers: A wider core reduces SBS threshold by enhancing A_{eff} .



Back

Close

Concluding Remarks

- Optical waveguides allow nonlinear interaction over long lengths.
- Optical fibers exhibit a variety of nonlinear effects.
- Fiber nonlinearities are feared by telecom system designers because they affect system performance adversely.
- Nonlinear effects are useful for many applications.
- Examples include: ultrafast switching, wavelength conversion, broadband amplification, pulse generation and compression.
- New kinds of fibers have been developed for enhancing nonlinear effects (photonic crystal and other microstructured fibers).
- Nonlinear effects in such fibers are finding new applications in fields such as optical metrology and biomedical imaging.



44/44

Further Reading

- G. P. Agrawal, *Nonlinear Fiber Optics*, 5th edition. (Academic Press, 2013).
- R. W. Boyd., *Nonlinear Optics*, 3rd edition (Academic Press, 2008).
- G. P. Agrawal, *Applications of Nonlinear Fiber Optics*, 2nd ed. (Academic Press, 2008).
- J. M. Dudley and J. R. Taylor, *Supercontinuum Generation in Optical Fibers* (Cambridge University Press, 2010).
- G. New, *Introduction to Nonlinear Optics* (Cambridge University Press, 2014).



45/44



Back

Close